# The Dynamic Controller Design of the Nuclear Steam Generator Water Level Control System

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## 증기발생기 디지탈 수위조절 시스템의 동적 제어기 설계

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#### ABSTRACT

The steam generator feedwater and level control system is designed by two steps of the feedwater control design and the feedback loop controller design. The feedwater servo system is designed by the optimal LQR/LQG approach and then is modified by the LTR method to recover the robustness. The plant characteristics are subject to change with the power variation and these dynamic properties are considered in the design of the feedback controller. All the designs are made in the continuous domain and are digitalized by applying the proper sampling period. The system is simulated for the two cases of power increase and decrease. From the results of simulation, it is found that the controller constants would rather be invariable during the power increase, while for the case of power decrease they should be changed with the power variation to keep the system stability.

Key words : Steam Generator, Level Control, LQR/LQG

### I. INTRODUCTION

The steam generator is one of important equipments in the nuclear power plant. It functions as a boundary between the primary and the secondary systems. It is a heat source to the secondary system and at the same time, it is a heat sink of the primary system. Therefore the steam generator should maintain the sufficient amount of water. However too much water raises the problem of moisture carry-over to the steam turbine, which is critical to the turbine life. Because of these problems,

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limitations are imposed both on the upper and lower bounds of water level. But it is very difficult to control the steam generator water level within the permissible span when the power is low. Particularly during the start up, a great attention should be paid by an operator. and the trip by breaching the level limitations is one of main causes of lowering the plant availability. Presently several systems<sup>(1),(2)</sup> are developed and installed to control the level automatically and show a good performance. But they are still PID based ones, while a number of important issues concerning controller design. robustness. the stability have been integrity and addressed by modern control theory.

In designing the feedwater control system, two points are to be considered. One is the uncertainty of plant and measurement, and the other is the limitation on the feedwater valve reflect motion. To these problems together in design, the optimal design of the LQR/LQG is preferable to the existing classical design. However, the optimal design stresses too much the minimization of the performance index. or cost function, and may rasie the problem of robustness. Therefore, the loop transfer recovery (LTR) method is used in this in this study to guarantee the performance robustness.

It should be noted that the of the thermal-hydraulic properties steam generator are subject to change with the power variations. In the studies<sup>(3),(4),(5)</sup>. the previous plant properties were described in terms of the power at which the transient starts and were assumed to be constant until the system reaches a new steady state. But in reality, all the plant characteristics change with the power variations, and these dynamic properties are taken into account in this study.

## II. LQG/LTR DESIGN OF FEEDWATER CONTROL SYSTEM

The steam generator feedwater and level control system is described in Fig.1. It employs three elements of system flow rate, feedwater flow rate and steam generator water level. The feedwater flow rate and the level signals are feedbacked, and are summed with the input signal of steam flow rate to generate a feedwater control signal. In addition, the steam flow rate, primary temperature and feedwater coolant temperature act on the steam generator as disturbance signals. As shown in the figure, the overall control system design can be divided into two steps, that is, the design of the feedwater station and the determination of the controller located on the feedback loop.



Fig. 1 Steam Generator Level Control System

Since the feedwater station is a servo system, it is a common practice to introduce an integrator to eliminate the steady state errors. By introducing the integrator gain and feedback gain, the feedwater servo system can be converted to the regulating system by variable transformation as follows.

$$\boldsymbol{\xi} = \boldsymbol{A}\boldsymbol{\xi} + \boldsymbol{B}\boldsymbol{w}, \quad \boldsymbol{\zeta} = \boldsymbol{C}\boldsymbol{\xi} + \boldsymbol{D}\boldsymbol{w}$$

$$\boldsymbol{w} = -\boldsymbol{K}\boldsymbol{\xi}$$
(1)

Equation (1) is a regulating system and the optimal feedback gain can be determined by the LQR (Liner Quadratic Regulating) method. With the state and input weighting matrices of Qand R, the ARE (Algebraic Riccati Equation) is

$$A^{T}P + PA + Q - PBR^{-1}B^{T}P = 0$$

$$Q = q(C^{T}C), R = rI$$
(2)

Then the optimal gains are determined as

$$\boldsymbol{K} = \boldsymbol{R}^{-1} \boldsymbol{B}^{T} \boldsymbol{P} = [K_{1} c - K_{2} a - K_{2} b]$$
(3)

The ratio of two weighting matrices has a strong influence on the system characteristics. For example, as rincreases, a greater penalty is imposed on the input energy and the system becomes more stable, but at the expense of slower speed. With the valve time constant of 1 sec, numerous values of q/r are checked with respect to various control specifications and traded off as q= r = 1. The gains are K = (0.2679)

(0.7321), or  $(K_1 K_2) = (1.0 \ 0.7231)$ , and the system poles are located at (-0.8660  $\pm j0.5$ ). The frequency responses show that the system has a sufficient margin of 81 degrees, which is the benefit of LQR design. It is well known that the feedwater measurement has a great uncertainty, particularly at the lower power levels, and the noised signal is not proper to be feedbacked. In this situation, it is desirable to build an optimal observer by the LQG (Linear Quadratic Gaussian) method to estimate the feedwater signal. But it is necessary to consider the robustness of the compensator designed by the LQG approach. The issue is that in any actual situation the plant dynamics may not be exactly known, and there may exist disturbances in the system. The compensator should provide not only good performance but also performance robustness in the face of disturbances and stability robustness in the presence of unmodeled plant dynamics.

In general, the LQG dynamic regulator has no guaranteed robustness<sup>(6)</sup>, in contrast with the LQR regulator which guarantees the robustness with infinite gain margin and more than 60 degrees phase margin. Other problems with the LQG is that requires statistical information of the noise process, which is either unavailable or is impractical to obtain in most cases. However, the robustness of the LQR hints that by selecting the design parameters of observer weighting matrices, the LQG can approximately recover the LQR properties. For the noised system, the

loop transfer function of the LQG is

$$\boldsymbol{M}(s)_{LQG}$$
  
=  $\boldsymbol{K}(s\boldsymbol{I} - \boldsymbol{A} + \boldsymbol{B}\boldsymbol{K} + \boldsymbol{L}\boldsymbol{C}^{-1}\boldsymbol{L}\boldsymbol{C}(s\boldsymbol{I} - \boldsymbol{A})^{-1}\boldsymbol{B}$   
=  $\boldsymbol{K}\boldsymbol{\Phi}_{r}(s)\boldsymbol{L}\boldsymbol{C}\boldsymbol{\Phi}_{0}(s)\boldsymbol{B}$   
(4)

Under the conditions of that the plant is non-minimum, the following relation can be derived by the matrix inversion lemma<sup>(7)</sup>.

$$\lim_{s \to \infty} \mathbf{M}(s)_{LQG} = \mathbf{M}(s)_{LQR} \tag{5}$$

Then by controlling the process noise spectral density, which is а kev parameter of the LQG design, the optimal observer gain is obtained by solving the relevant Riccati equation. As the LQG weighting, that is  $Q_0 = q^2 B B^{T}$ , increases, the LQR target feed loop is recovered. From these results. q is determined as 150 and the observer gain is L = (16.35, 150). The phase margin is about 77 degress and the observer poles are located at  $(-8.6747 \pm$ j8.6458), which shows a faster speed than that of the system. The feedwater controller designed so far, in the form of transfer function, is

$$H(s) = \frac{114.1884s + 150}{s^2 + 18.0814s + 162.9686}$$
(6)

## III. SYSTEM CONTROLLER ON THE LEVEL FEEDBACK LOOP

There are four inputs which act on

the steam generator, that is, feedwater flow rate, steam flow rate, primary coolant temperature and feedwater temperature. The open loop transfer function between each of these inputs and the level is a function of power. In the previous studies<sup>(4)(5)</sup>, the transfer functions were determined by the steady state power at which a transient starts and were assumed to be constant during the transient.

The general approach to the control system design is a trade off the conflicting control specifications such as stability. For system speed and example, if a system is unstable, the gain should be decreased to keep the stability. On the other hand, when the system has a sufficient stability, it is desirable to increase the gain to speed up the system. It is the same for the steam generator. The steam generator is unstable at low power, but becomes more stable with the increase of power. Therefore it may be too conservative to keep the same control constants during the power increase because the system shifts into the stable region. On the contrary, the system may become unstable for the case of power decrease since it gets into the unstable region. On account of these facts, a controller whose control constants change continuously to reflect the varying plant characteristics during the transient is considered, and is to be named dynamic controller hereinatfer.

The overall dynamic steam generator level and feedwater control system is outlined in Fig. 2.



Fig. 2 Power Dependent Steam Generator Level Control System

The system is MIMO (multi input multi output). The steam flow rate is input to the system as a command signal and the outputs are power level. The level signal is feedbacked and summed with the input signal. The feedback loop of the feedwater is embedded in the feedwater station. It is to be noted that the steam flow rate signal goes directly generator to the steam with other disturbance signals of the primary coolant and feedwater temperatures. The power signal changes the characteristics of steam generator, and the controller is to be modulated by the power. This relation is described by dotted lines.

Figure 3 is the same as Fig. 2, but is described in MISO (multi input single output) by using the transfer function blocks which depend on the power. The  $\Delta U_i(s)$ , where i = 2, 3, 4. indicates the input signal of the steam flow rate, primary coolant temperature, and feedwater temperature, respectively, and  $H_i(s)$  is the transfer function which corresponds to each input and is a function of power.





It should be understood clearly that the system is a regulating system in that the level should maintain the predetermined value regardless of the changes. input signal And for а regulating system, with the condition of controllability, it is possible to build a LOQ controller which compensates off the disturbance signals to make the input energies to the plant zero. However, since the steam flow rate acts on the plant directly, or physically the steam always comes out from the plant. it has no sense to compensate off the input signal the LOQ feedback by signals. and the overall control structure should be such the one as described Fig. 3 using in a PID controller. From Fig. 3 the feedwater flow rate to the steam generator and the level output are

 $\Delta W_{f}(s)$   $= \frac{\Delta W_{s}(s) F(s)(1 - C(s)H_{2}(s)) - F(s)O(s)}{1 + F(s)H_{1}(s) C(s)}$   $\Delta L(s)$   $= \frac{\Delta W_{s}(s) (H_{2}(s) + F(s)H_{1}(s)) + O(s)}{1 + F(s)H_{1}(s)C(s)}$  (7)

The transfer function  $H_i(s)$  in the above equations are subject to change continuously with the power, and the power should be determined first to obtain the feedwater flow rate and level. For the calculations, the relationship between each input,  $\Delta U_i(s)$ , and the power variation,  $\Delta P(s)$ , has been derived in the from of transfer function as below.

$$P_i(s) = \frac{\triangle P(s)}{\triangle U_i(s)} \tag{8}$$

where i = 1, 2, 3, 4 and indicates the feedwater and steam flow rates, primary coolant and feedwater temperatures, respectively.



Fig. 4 Power Variation for Unit Step Change of Feedwater Flow Rate

The thermal-hydraulic code developed in Ref.(3) is used to determined the Eq.(8). It is found that the power variation itself is a function of power also. For example, Fig. 4 shows the responses of power variation for unit step increase of the feedwater flow.

The solid lines are results of the code calculation and dotted lines are by the Laplacian inversion of  $P_1(s)$ . As the power becomes lower. the output response gets unstable. In defining  $P_i(\mathbf{s})\mathbf{s}$ . typical and simple transfer functions of the first and the second order forms are used. The more exact description is possible with the higher order function, but they introduce the increase of state order and it takes a long time to calculate.

The controller on the level feedback loop, C(s), is an ordinary PID controller. But the system speed is slow enough to neglect the differentiator, and the controller constants of gain and integration time are determined as<sup>(5)</sup>

$$C(s) = K \left( \frac{1 + T_1 s}{T_1 s} \right)$$
  

$$K = 34.3 + 3.85P + 0.2P^2$$
(9)  

$$T_1 = 64.13 - 60P + 2.1P^2$$

where P is the initial power. The control constants of above equation were determined under the constraint of that the overall system should have the phase margins of more than 30 degrees for any initial power, and the gain can be increased with the power. However, if the constants are held constant during the power decrease, the system gets unstable. The initially determined gain is too large to maintain the stability since the plant characteristics becomes more unstable as the power decreases.

## IV. SIMULATION

The feedwater controller and the level feedback controller are designed in the continuous s-domain. and it is necessary to digitalize them for the actual use. The digitalization of the continuous controller already designed is so called an indirect method. This method has an advantage of the simplicity, but since the discretization schemes are always approximations, the resulting digital controller may be different from the original continuous one. The degree of approximation depends on the sampling period which is key parameter in converting a а continuous system to a digital system<sup>(9)</sup>.

The selection of the sampling period is made based on the speeds of the plants which comprises the system. It is found that the speeds of the system are very slow, which is the general property of the thermal-hydraulic processes<sup>(10)</sup>. For example, the natural frequency, which is the direct index of the speed, of the system ranges from about 0.01 to 0.5 rad/sec depending on the power. This means that the system is not so sensitive to the sampling period. For the case of feed water station, the Bode diagram in w-domain indicates that the bandwidth is 1.07 rad/sec, which is faster than the system. Therefore, from the Nyquist frequency condition, the upper bound of the sampling period is determined as about 3.4 seconds.

In general, it is thought that there is no limitation on the lower bound of the sampling period, which is not always true. If the period is too small, the controllability matrix of the discretized system may not satisfy the rank condition and the system properties become different from those of original system<sup>(7)</sup>. From the Bode plots for various sampling periods, the sampling period is determined as 1 second, which is used in all the simulations below.

For the simulations, the system described in Fig. 3 is used. All the continuous plants are discretized by introducing the ZOH (zero order holder) transformation while the controllers are the Tustin transformation. bv The calculation procedure is such that the power at a given moment is obtained first from the duplicated scheme of Fig. 3 in which  $H_i(s)s$  are replaced by  $P_i(s)s$ and then this power is used to determine the new  $H_i(s)s$  and  $P_i(s)s$  for the next time step. The overall system is converted to a set of state equations and the dimension of the system matrix is 19 by 19. The state equations are solved by MATLAB<sup>(11)</sup> at each time step.

The input conditions are the same as those of Refs.[4] and [5]. That is, for the power increase from 5 to 10%, the steam flow rate is increased linearly at the rate of 0.273 kg/sec from t = 10 to 70 second, and the primary temperature is increased linearly by 0.03°C from t =25 to 70 second and again by 0.026°C from t = 70 to 80 second. There is no feedwater temperature change in the power range of 5 to 10%.

Two cases are considered in numerical simulations. One is the case of which that the plants of  $H_i(s)s$  and  $P_i(s)s$  are

subject to change continuously with the but the control power variation constants of C(s) are fixed to the values which are determined by the initial This case is to be named power. semi-dynamic run in this paper. The other, which is named dynamic run, is the case of which the controller constants, as well as  $H_i(s)s$  and  $P_i(s)s$ . change with the power.



Fig. 5 (a) Transients of Level Variation. 5% to 10% Power Increase



Fig. 5 (b) Transients of Power Variation, 5% to 10% Power Increase



Fig. 5 (c) Transients of Feedwater Variation. 5% to 10% Power Increase



Fig. 5 (d) Transients of Gain Variation. 5% to 10% Power Increase

Figures 5(a) through (d) show the variations of the level, feedwater flow rate, power and controller gain for the case of semi-dynamic as well as for the dynamic calculation. Also shown are the results of previous study<sup>(5)</sup> in which the plant and controller were assumed to be constant during the transients (non-dynamic).

First, it can be found that the peak water levels both of the semi-dynamic

and dynamic cases are less than those of non-dynamic case. Those peak values are more realistic since the plant changes in a real situation. Particularly, the feedwater variation of the semidynamic case shows a milder response. The results of dynamic run are not so good as those of semi-dynamic run. although they are stable. This is because the dynamic controller gain which is determined from Eq.(9)bv using P(t), instead of the initial power, increase too much with the power.

For the case of power decrease, although its detail results are not shown here, the simulation results show the overall phenomena inverse to the power increase. But the results of dynamic run show the milder transients than that of semi dynamic run.

## V. CONCLUSION

The steam generator feedwater and level control system is designed by two steps. The controller of the feedwater servo system is determined first and then the controller on the level feedback loop is considered. The feedwater controller design is made by LQR method to consider the constraints on the both the states and the input energy. On account of the uncertainties of the system and measurement noises. an observer is constructed by the LTR approach since the ordinary LQG method does not guarantee the system robustness. The controller designed by this method shows a good robustness in the presence of severe system The constants perturbations. of the controller on the feedback loop is determined to maintain the same stability margin for all power levels.

Since all the transfer functions between the input signals to the steam generator level are subject to change with the power variations, the relations between input signals and their corresponding output of power variation are described in the simple form of transfer functions. The power variation is then used to determine the new transfer functions and the values of feedback loop controller constants. For the digitalization of the controller, the sampling period. which is а kev parameter of the digital design, is determined as 1 second by investigating the speed and system frequency responses. Two kinds of simulations are made. The first is the case of which all the properties of plants are varying but with power with the fixed controller, and the second is the case of which the controller, as well as the plants, changes with power. From the results of simulation, it is found that the constant controller is desirable during the power increase, but the controller constants should be changed with the power variation for the case of power decrease.

#### VI. 요 약

증기발생기의 급수 및 수위조절 관련하여 전 체 시스템을 급수 서보 시스템과 궤환 제어기로 나누어 설계하였다. 급수시스템의 설계에는 최 적제어이론을 사용하였으며 시스템의 온전성을 위하여 다시 LTR 기법을 이용하였다. 증기발 생기의 제어특성은 열수력적인 이유에 의하여 출력에 따라 계속적으로 변하게 되므로 궤환제 어기가 이러한 변화를 동적으로 반영할 수 있도 록 하였다. 모든 설계는 연속시스템에서 이루어 졌으며 적절한 샘플링 주기를 선정하여 디지탈 화 하였다. 이같은 시스템을 이용하여 출력 증 가 및 감소의 두가지에 대해 검토한 결과, 출력 의 증가시에는 제어상수를 고정시키는 것이 바 람직하나 출력의 감소시에는 시스템의 안정을 위하여 제어상수가 출력에 따라 동적으로 변화 해야 함을 알 수 있었다.

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